



Effective description of squark interactions

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J.G., Siannah Peñaranda, Raúl Sánchez-Florit, JHEP 0904:016,2009, arXiv:0812.1114

- 1 Introduction
 - Standard Model
 - Experiments
 - Supersymmetry
- 2 Sfermion Decays to charginos/neutralinos
- 3 Yukawa-effective couplings
- 4 Logarithmic terms
- 5 Effective Theory
- 6 Conclusions

The Standard Model

- Present paradigm of elementary particles composition and interactions
- Gauge theory
 - $SU(3)_c \otimes SU(2)_L \otimes U(1)_Y$
 - Spontaneous Symmetry Breaking $SU(2)_L \otimes U(1)_Y \Rightarrow U(1)_Q$
 \Rightarrow Massive gauge bosons: M_Z, M_W
- Probed at the 10^{-3} level at LEP, SLD, Tevatron, ...
- Theoretical problems: hierarchy problem
- Prepared for whatever new physics might appear at Experiments!
 \Rightarrow Study possible extensions of the SM

Missing: Higgs boson

- Experimental determination SSB
- Last (and necessary) building block of the Standard Model
 - or any electroweak gauge theory with massive gauge bosons

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Experiments

Tevatron II: $p\bar{p}$ @ $\sqrt{S} = 2\text{TeV}$

- Well, and running, and providing interesting results! (single top, Higgs exclusions, B -physics, ...)
- Marginal role in (direct) SUSY search.

The Large Hadron Collider: pp @ $\sqrt{S} = 14\text{TeV}$

- Start: autumn 2009
- $M \leq 2.5\text{ TeV}$ (\tilde{q}, \tilde{g}). Measurement of properties.

Higgs boson

Standard Model: Discovery guaranteed in the range 114 – 1000 GeV

International Linear Collider: e^+e^- @ $\sqrt{S} = 0.5 - 1.5\text{TeV}$

- Planning stage: <http://www.linearcollider.org>
- High precision measurements, $M \leq \sqrt{S}/2$

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Supersymmetry

Supersymmetry (SUSY) ...

- ... is **the** extension of the Poincaré symmetry of space-time
- ... leads to a symmetry between fermions & bosons

Gauge theory with minimal SUSY:

- **same number of fermionic & bosonic degrees of freedom**
 - ⇒ a superpartner of different spin exists for each particle
- **couplings are correlated**
 - ⇒ e.g. scalar 4-point int. \leftrightarrow gauge couplings
- **superpartners have the same mass**
 - ⇒ SUSY must be broken at the electroweak scale

Gauge theory with broken SUSY

- **superpartner masses** enter as **additional free parameters** (essentially)

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Gauge theory with broken SUSY

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- Existence of a light Higgs boson, $M_{h^0} \lesssim 130 \text{ GeV}$.

M. Carena *et al.*, *Nucl. Phys.* **B 580** (2000) 29 [hep-ph/0001002].

J.R. Espinosa, R. Zhang, *JHEP* **0003** (2000) 026, [hep-ph/9912236].

- SUSY models predictions are not in contradiction with high precision EW data.

MSSM: Minimal Supersymmetric Standard Model

gauge group: $SU(3)_c \times SU(2)_I \times U(1)_Y$

Regular particles	Spin	Superfields	Spin	superpartners
fermions quarks $u d s c b t$ leptons $e \nu_e \mu \nu_\mu \tau \nu_\tau$	$\frac{1}{2}$	$\hat{Q} = \begin{pmatrix} \hat{u}_L \\ \hat{d}_L \end{pmatrix}, \hat{D} = \hat{d}_R^c, \hat{U} = \hat{u}_R^c$ $\hat{L} = \begin{pmatrix} \hat{\nu}_L \\ \hat{e}_L \end{pmatrix}, \hat{E} = \hat{e}_R^c$	0	sfermions squarks $\tilde{u} \tilde{d} \tilde{s} \tilde{c} \tilde{b} \tilde{t}$ sleptons $\tilde{e} \tilde{\nu}_e \tilde{\mu} \tilde{\nu}_\mu \tilde{\tau} \tilde{\nu}_\tau$
Gauge Bosons G, W^\pm, Z, γ	1	$\hat{G}, \hat{W}^\pm, \hat{Z}, \hat{\gamma}$	$\frac{1}{2}$	gauginos $\tilde{G}, \tilde{W}^\pm, \tilde{Z}, \tilde{\gamma}$
Higgs bosons H_u, H_d	0	$\hat{H}_d = \begin{pmatrix} \hat{H}_d^0 \\ \hat{H}_d^- \end{pmatrix}, \hat{H}_u = \begin{pmatrix} \hat{H}_u^+ \\ \hat{H}_u^0 \end{pmatrix}$	$\frac{1}{2}$	Higgsinos \tilde{H}_u, \tilde{H}_d

H_u, H_d lead to 5 physical Higgs bosons: h^0, H^0, A^0, H^+, H^-

$\tilde{W}^\pm, \tilde{Z}, \tilde{\gamma}$ and $\tilde{H}_u, \tilde{H}_d \rightarrow$ 2 charginos χ_1^+, χ_2^+ ; 4 neutralinos $\chi_1^0, \dots, \chi_4^0$

MSSM: Minimal Supersymmetric Standard Model

$\tan \beta$

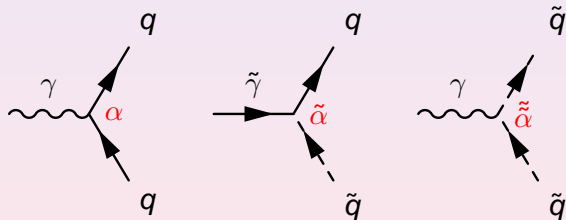
- Two neutral Higgs \rightarrow two vacuum expectation values: v_u, v_d
- $M_W^2 \sim v_u^2 + v_d^2$
- $\tan \beta = \frac{v_u}{v_d}$
- β is a mixing angle in the Higgs sector (together with α)
- potential large Yukawa couplings of bottom quarks

Gauge bosons G, W^\pm, Z, γ	1	$\hat{G}, \hat{W}^\pm, \hat{Z}, \hat{\gamma}$	$\frac{1}{2}$	gauginos $\tilde{G}, \tilde{W}^\pm, \tilde{Z}, \tilde{\gamma}$
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Determination of particle properties

- If new particles are found: what are they? (which model do they belong?)
 - ⇒ Check model predictions: obey their properties SUSY relations?
 - ⇒ Check precision predictions at the same level as SM
- SUSY: SUSY particle couplings are the same as SM



- $\alpha = \tilde{\tilde{\alpha}}$: charge of particle \tilde{q}
- $\alpha = \tilde{\alpha}$: genuine SUSY prediction

Sfermion Decays to charginos/neutralinos

- Check of SUSY: equality of particles and sparticles couplings
 - Can not be checked on S -channel pair-production
- In this work we concentrate on fermionic decays of sfermions

$$\tilde{f} \rightarrow f^{(\prime)} \chi^{(0,+,-)}$$

- Some of these decays channels are *always* available: $\tilde{b} \rightarrow b \chi_1^0$. χ_1^0 is usually the Lightest SUSY Particle (LSP).
- Whenever open, some of these channels have a non-negligible Branching Ratio.
- Previous computations: Full one-loop QCD and Electroweak corrections are available

S. Kraml *et al.*, *Phys. Lett.* **B386** (1996) 175, [hep-ph/9605412](#).

A. Djouadi, W. Hollik, C. Jünger, *Phys. Rev.* **D55** (1997) 6975, [hep-ph/9609419](#).

J. G., Ph.D. Thesis, UAB 1999.

J. G., W. Hollik, J. Solà, *Phys. Lett.* **B437** (1998) 88, [hep-ph/9802329](#). *JHEP* **0210** (2002) 040, [hep-ph/0207364](#)

⇒ large corrections and **non-decoupling** effects

- To compare with experiment we need:
 - Precision predictions **AND** good approximations

- Recompute the QCD corrections to squark decays
- Find the leading terms of the corrections
- Perform a renormalization group analysis, and compare with the one-loop result
 - ⇒ asses the precision of the **running coupling** approximation
- Combine the one-loop and renormalization-group computations

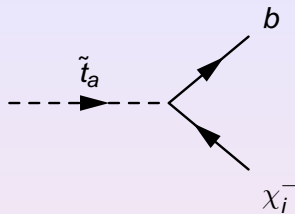
Tree-level interactions

[Example: top-squark \rightarrow bottom chargino]

$$\mathcal{L}_{\chi_r \tilde{f}_a f'} = -g \tilde{f}_a^* \tilde{\chi}_r \left(A_{+ar}^{(f)} P_L + A_{-ar}^{(f)} P_R \right) f' .$$

$$A_{+ai}^{(t)} = R_{1a}^{(t)} V_{i1}^* - \lambda_t R_{2a}^{(t)} V_{i2}^* ,$$

$$A_{-ai}^{(t)} = -\lambda_b R_{1a}^{(t)} U_{i2} ,$$



- gauge couplings: g
- Yukawa couplings: $\lambda_{t,b} = \frac{m_{t,b}}{v_{2,1}} = \frac{m_{t,b}}{\sqrt{2}M_W \{\sin, \cos\} \beta}$
- Squark mixing matrices: R
- Chargino mixing matrices: U, V
- Chirality projectors: $P_{L,R}$
- 2 squarks: $a = 1, 2$ and 2 charginos $i = 1, 2$

Yukawa-effective couplings

- QCD \oplus SUSY Higgs physics

\Rightarrow Running mass \oplus SUSY threshold corrections

$$\lambda_b^{\text{eff.}} \equiv \frac{m_b^{\text{eff.}}}{v_1} \equiv \frac{m_b(Q)}{v_1(1 + \Delta m_b)} , \quad \lambda_t^{\text{eff.}} \equiv \frac{m_t^{\text{eff.}}}{v_2} \equiv \frac{m_t(Q)}{v_2(1 + \Delta m_t)} ,$$

$$\Delta m_b^{\text{SQCD}} = \frac{2\alpha_s}{3\pi} m_{\tilde{g}} \mu \tan \beta I(m_{\tilde{b}_1}, m_{\tilde{b}_2}, m_{\tilde{g}}) ,$$

$$\Delta m_t^{\text{SQCD}} = \frac{2\alpha_s}{3\pi} m_{\tilde{g}} \frac{\mu}{\tan \beta} I(m_{\tilde{t}_1}, m_{\tilde{t}_2}, m_{\tilde{g}}) , \quad (1)$$

$$I(a, b, c) = \frac{a^2 b^2 \ln(a^2/b^2) + b^2 c^2 \ln(b^2/c^2) + c^2 a^2 \ln(c^2/a^2)}{(a^2 - b^2)(b^2 - c^2)(a^2 - c^2)} .$$

- Total decay widths Γ and relative corrections δ
- One-loop
- Yukawa-effective
- Yukawa-Improved:
 - Combination of: Effective couplings \oplus one-loop
 - Contains: Higher order effects \oplus kinematic effects
- δ -remainder: One loop effects **NOT** described by the effective couplings

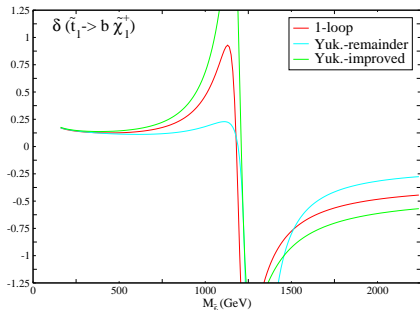
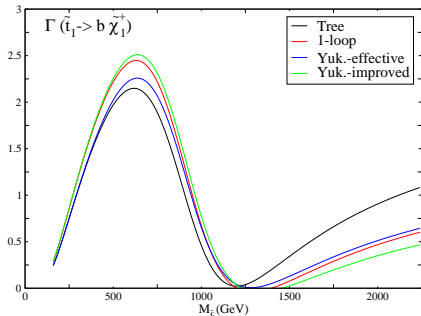
$$\begin{aligned}\tan \beta &= 5, \quad \mu = 300 \text{ GeV}, \quad M = 200 \text{ GeV}, \quad M_{\tilde{f}_L} = 800 \text{ GeV}, \\ m_{\tilde{g}} &= 3000 \text{ GeV}, \quad M_{SUSY} \equiv M_{\tilde{f}_R} = 1000 \text{ GeV}, \\ A_t = A_b &= 2M_{\tilde{f}_L} + \mu / \tan \beta = 1660 \text{ GeV},\end{aligned}$$

$$M_{\chi^+} = (170.40, 337.50) \text{ GeV},$$

$$M_{\chi^0} = (89.52, 172.28, 305.46, 338.58) \text{ GeV},$$

$$m_{\tilde{b}} = (802.05, 1000.30) \text{ GeV},$$

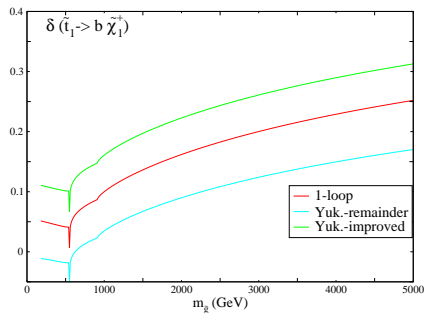
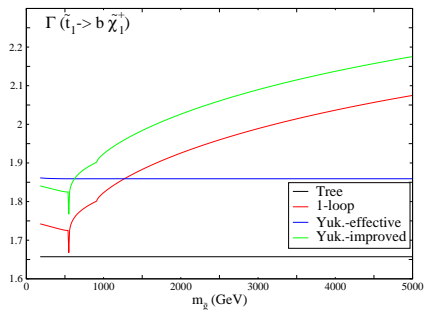
$$m_{\tilde{t}} = (720.55, 1084.25) \text{ GeV}.$$



At $M_{\tilde{f}_L} \sim 1250 \text{ GeV}$:

- $\Gamma^{\text{tree}} \sim 0 \Rightarrow \Gamma^{1\text{-loop}} < 0$
- $\Gamma^{\text{eff}} > 0$ (by definition)
- Non-perturbative behaviour can not be described by effective theory
 - \Rightarrow Region **not** interesting phenomenologically!

Gluino Mass



- One-loop $\sim \log m_{\tilde{g}}$

Not reproduced by Yukawa-effective

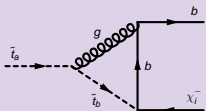
- Large remainder corrections, with non-flat behaviour

Logarithmic terms: where do they come from?

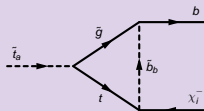
Fundamental

- SUSY: $\alpha = \tilde{\alpha}$
- SUSY is **broken** (by $m_{\tilde{g}}$)
 - $\Rightarrow \alpha \neq \tilde{\alpha}$
 - $\Rightarrow \alpha - \tilde{\alpha} \simeq \log(\Lambda_{\text{SUSY-breaking}}) \simeq \log m_{\tilde{g}}$

One-loop



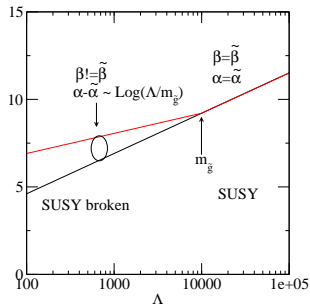
$$\Delta_\varepsilon + \log \mu_D / M_1$$



$$\Delta_\varepsilon + \log \mu_D / M_2 = \log M_1 / M_2$$

- If we **remove gluinos** ($m_{\tilde{g}} \rightarrow \infty$) \Rightarrow Divergent result $\Rightarrow \log m_{\tilde{g}}$

Effective Theory

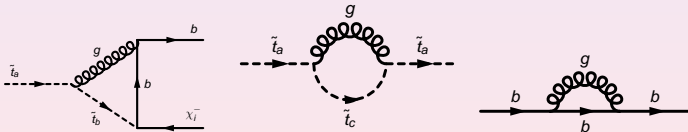


- At $Q > m_{\tilde{g}}$: SUSY theory: $\alpha = \tilde{\alpha}$ gauge and gaugino couplings run equal $\beta = \tilde{\beta}$
- At $Q < m_{\tilde{g}}$ SUSY broken: the β functions are different: $\beta \neq \tilde{\beta}$
 $\Rightarrow \tilde{\alpha} - \alpha \sim (\tilde{\beta} - \beta) \log m_{\tilde{g}}$

Effective Theory

Construct an effective theory:

- $Q > m_{\tilde{g}}$: SUSY theory ($q, \tilde{q}, \chi^-, g, \tilde{g}$):
 - Chargino couplings are given by the SUSY relations
- $Q < m_{\tilde{g}}$: broken SUSY (q, \tilde{q}, χ^-, g) – **no gluinos**
 - Compute the QCD running of the chargino couplings from the matching scale ($m_{\tilde{g}}$) down to the process scale (Q)
 - Only contributions from gluons!



$$A(Q) = A(m_{\tilde{g}}) \left(\frac{\alpha_s(Q)}{\alpha_s(m_{\tilde{g}})} \right)^{2/\beta_0}$$

β_0 : QCD β -function

- Now we have to compute $A(m_{\tilde{g}})$: $A(m_{\tilde{g}}) = H(m_{\tilde{g}}) + G(m_{\tilde{g}})$

$H(m_{\tilde{g}})$: Higgs coupling ($\lambda_{b,t}$): runs as the mass:

$$\begin{aligned} \lambda(m_{\tilde{g}}) &= \lambda(Q) \left(\frac{\alpha_s(m_{\tilde{g}})}{\alpha_s(Q)} \right)^{4/\beta_0} \\ H(Q) &= H(m_{\tilde{g}}) \left(\frac{\alpha_s(Q)}{\alpha_s(m_{\tilde{g}})} \right)^{2/\beta_0} \\ &= \lambda(Q) \left(\frac{\alpha_s(Q)}{\alpha_s(m_{\tilde{g}})} \right)^{-2/\beta_0} \\ &\simeq \lambda(Q) \left(1 + \frac{\alpha_s(Q)}{\pi} \log \frac{Q}{m_{\tilde{g}}} \right) \end{aligned}$$

$G(m_{\tilde{g}})$: gauge coupling (g): It does not run due to QCD

$$\begin{aligned} G(m_{\tilde{g}}) &= g(0) \\ G(Q) &= G(m_{\tilde{g}}) \left(\frac{\alpha_s(Q)}{\alpha_s(m_{\tilde{g}})} \right)^{2/\beta_0} \\ &= g \left(\frac{\alpha_s(Q)}{\alpha_s(m_{\tilde{g}})} \right)^{2/\beta_0} \\ &\simeq g \left(1 - \frac{\alpha_s(Q)}{\pi} \log \frac{Q}{m_{\tilde{g}}} \right) \end{aligned}$$

Effective chargino/neutralino couplings

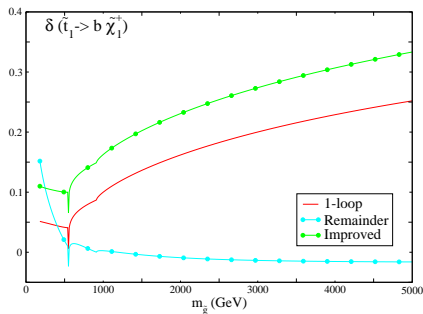
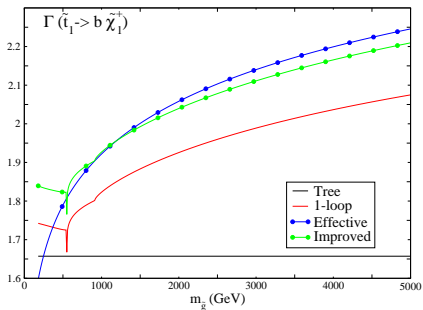
$$g^{\text{eff.}}(Q) = g \left(\frac{\alpha_s(Q)}{\alpha_s(m_{\tilde{g}})} \right)^{\frac{2}{\beta_0}} \simeq g \left(1 - \frac{\alpha_s(Q)}{\pi} \log \frac{Q}{m_{\tilde{g}}} \right),$$

$$\tilde{\lambda}_{b,t}^{\text{eff.}}(Q) = \lambda_{b,t}^{\text{eff.}}(Q) \left(\frac{\alpha_s(Q)}{\alpha_s(m_{\tilde{g}})} \right)^{\frac{-2}{\beta_0}} \simeq \lambda_{b,t}^{\text{eff.}}(Q) \left(1 + \frac{\alpha_s(Q)}{\pi} \log \frac{Q}{m_{\tilde{g}}} \right),$$

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- Define again: effective, remainder, ...

Gluino Mass



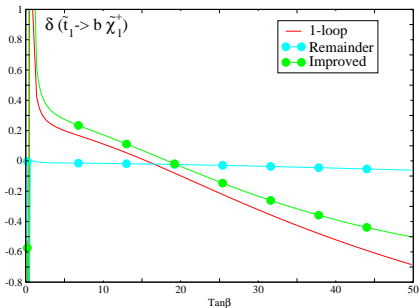
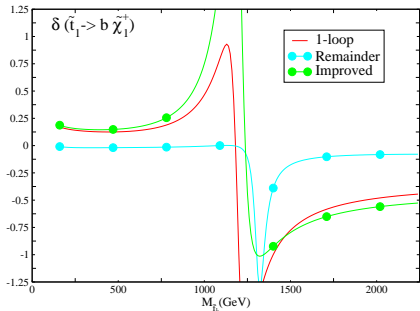
- The **Effective** description follows the logarithmic behaviour of the **one-loop**
 - The **Remainder** contributions tend to zero at large gluino mass
- ⇒ The effective description gives a good approximation to the one-loop behaviour

Behaviour checked for:

- All squark decay channels into charginos/neutralinos
- Change in any input parameter ($m_{\tilde{g}}, \tan \beta, \dots$)

In all cases:

- **Remainder** corrections decrease after including the $\log m_{\tilde{g}}$ terms
⇒ better approximation than only Yukawa-effective
- **Remainder** corrections stay flat under variations of parameters
⇒ are a good approximation to the one-loop behaviour
- **Except:**
 - Corners of the parameter space where: $\Gamma^{tree} \rightarrow 0$
⇒ Phenomenologically uninteresting



- Effective description of squark interactions
 - Running mass \oplus threshold corrections
 - Additional $\log m_{\tilde{g}}$ term
- Describes correctly squark decays
- Easy/cheap to include in Monte-Carlo simulations
- Non-decoupling behaviour:
 - Due to breaking of SUSY
- \Rightarrow Deviation of SUSY prediction: $\alpha = \tilde{\alpha}$!
- Future
 - Generalize this description to every SUSY process

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$\tan \beta$					
	$\tan \alpha, m_{H^0}$ \uparrow M_{H^\pm}				
$\begin{pmatrix} \nu_e \\ e^- \end{pmatrix} \cdots \begin{pmatrix} t' \\ b' \end{pmatrix}$	H_1, H_2	B	W	g	$R = 0$
$\begin{pmatrix} \nu_e \\ e^- \end{pmatrix} \cdots \begin{pmatrix} t \\ b \end{pmatrix}$	H^\pm, A^0, H^0, h^0	γ, Z, W^\pm		g	
$\begin{pmatrix} \tilde{\nu}_e \\ \tilde{e}_L^-, \tilde{e}_R^- \end{pmatrix} \cdots \begin{pmatrix} \tilde{t}_L, \tilde{t}_R \\ \tilde{b}_L, \tilde{b}_R \end{pmatrix}$	\tilde{h}_1, \tilde{h}_2	\tilde{B}	\tilde{w}	\tilde{g}	$R = 1$
$\begin{pmatrix} \tilde{\nu}_e \\ \tilde{e}_1^-, \tilde{e}_2^- \end{pmatrix} \cdots \begin{pmatrix} \tilde{t}_1, \tilde{t}_2 \\ \tilde{b}_1, \tilde{b}_2 \end{pmatrix}$	$\chi_{\{1,2\}}^-, \chi_{\{1,\dots,4\}}^0$			\tilde{g}	
	$m_{\tilde{b}_1}, m_{\tilde{b}_2}, m_{\tilde{t}_1}$ A_b, A_t (θ_b, θ_t)	M'	M	$m_{\tilde{g}}$	
	μ				
$\tan \beta$					

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$\begin{pmatrix} \nu_e \\ e^- \end{pmatrix} \cdots \begin{pmatrix} t' \\ b' \end{pmatrix}$	H_1, H_2	B	W	g	$R = 0$

- Main parameter: $\tan \beta = \frac{v_2}{v_1}$
 \Rightarrow Potential large Yukawa couplings of bottom quarks
- Squark mixing $\propto m_q$
 \Rightarrow only \tilde{t} (and \tilde{b} at large $\tan \beta$) can have large mass splitting.

$\begin{pmatrix} \tilde{\nu}_e \\ \tilde{e}_1^-, \tilde{e}_2^- \end{pmatrix} \cdots \begin{pmatrix} \tilde{t}_1, \tilde{t}_2 \\ \tilde{b}_1, \tilde{b}_2 \end{pmatrix}$	$\chi_{\{1,2\}}^-, \chi_{\{1,\dots,4\}}^0$			\tilde{g}
$m_{\tilde{b}_1}, m_{\tilde{b}_2}, m_{\tilde{t}_1}$ A_b, A_t (θ_b, θ_t)		M'	M	$m_{\tilde{g}}$
μ				
$\tan \beta$				