

Spontaneous parity violation in hot and dense baryon matter in QCD motivated hadronic models

A.A. Andrianov

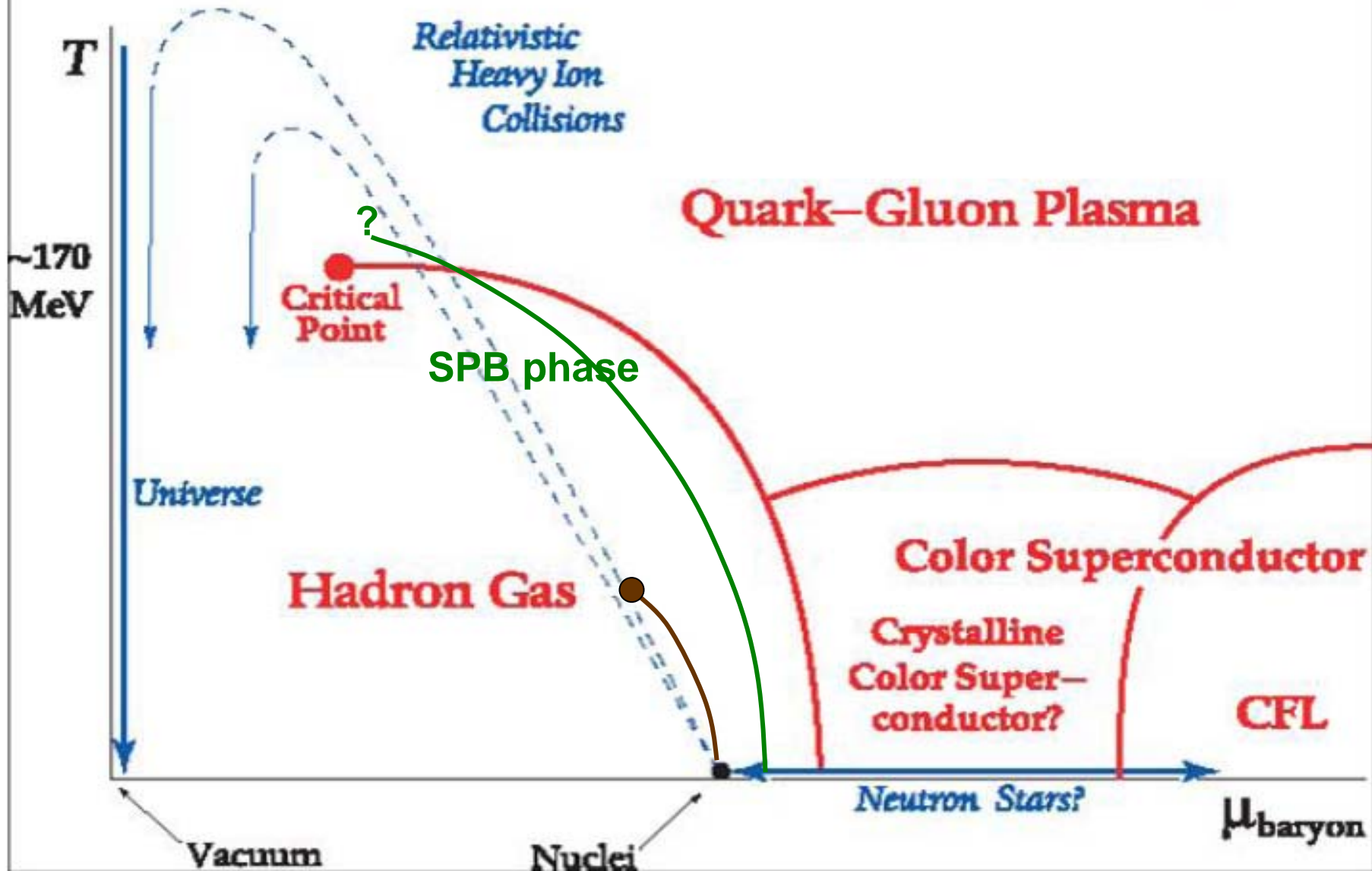
Sankt-Petersburg State University & Universitat de Barcelona

ICCUB (Institut de Ciències del Cosmos, Universitat de Barcelona)



**A.A. & D.Espriu, Phys.Lett.B, 663 (2008) 450;
A.A., V.Andrianov & D.Espriu, 0904.0413 [hep-ph]**

EXPLORING the PHASES of QCD



We guess **P- violation** to occur **at nearly zero** temperature but **large** baryon number density due to **condensation** of parity-odd mesons (pions, kaons,... and their heavy twins)

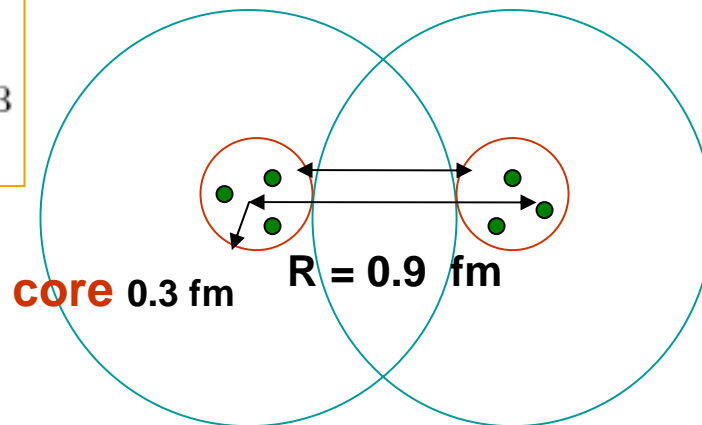
$$\rho_B \gg \rho_N \simeq 0.17 \text{ fm}^{-3} = (1.8 \text{ fm})^{-3}$$

How large?

Beyond the range of validity of pion-nucleon effective Lagrangian but not large enough for quark percolation, $\rho_B \sim (3 \div 8)\rho_N$ *i.e.* in the hadronic phase with **heavy meson** excitations playing an essential role in dense nuclear matter where quark-nuclear matter duality can be effectively used.

Example

$$\rho_B = 8\rho_N \simeq (0.9 \text{ fm})^{-3}$$



Higher-mass mesons + dressed quarks

$$R_{\pi, \sigma, \omega, \rho, \pi', \sigma' \dots} = (0.3 - 0.4) \text{ fm} = (500-700 \text{ MeV})^{-1}$$

Effective lagrangian approach

Low energies \implies Chiral lagrangian for pions:

$$\mathcal{L}_\pi = \frac{1}{4} F_\pi^2 \text{Tr} \left(D_\mu U^\dagger D^\mu U + m_\pi^2 (U + U^\dagger) \right)$$

$$U = \exp \left(i \frac{\pi^a \tau^a}{F_\pi} \right)$$

$$D_\mu U = \partial_\mu U + [V_\mu U]$$

Vector field

Density vs. chemical potential

(symmetric nuclear matter)

$$\langle N^\dagger N \rangle \iff \int d^3x \mu_B (\bar{N} \gamma_0 N(x) - \rho_B)$$

Corresponds to singlet vector current!

$$\mu_B \Rightarrow V_0$$

Disappears from pion lagrangian?

No! It is hidden in structural constants and masses.

$$F_\pi^2(\mu_B) \quad m_\pi^2(\mu_B)$$

We need a model of formation for these parameters:

QCD ?

At least an extension to QCD motivated Linear sigma models and/or Quark models !

From the hadron side heavy meson states are in game!

Extended linear sigma model
with two multiplets of scalar and pseudoscalar mesons
(with matching to QCD and to nuclear matter as much as possible)

$$H_j = \sigma_j \mathbf{I} + i\hat{\pi}_j, \quad j = 1, 2; \quad H_j H_j^\dagger = (\sigma_j^2 + (\pi_j^a)^2) \mathbf{I}, \quad \hat{\pi}_j \equiv \pi_j^a \tau^a$$

Chiral limit \longrightarrow $SU_L(2) \times SU_R(2)$ **symmetry**

“Quark/nuclear matter free energy” after bosonization

$$V_{\text{eff}} = \frac{1}{2} \text{tr} \left\{ - \sum_{j,k=1}^2 H_j^\dagger \Delta_{jk} H_k + \lambda_1 (H_1^\dagger H_1)^2 + \lambda_2 (H_2^\dagger H_2)^2 + \lambda_3 H_1^\dagger H_1 H_2^\dagger H_2 \right. \\ \left. + \frac{1}{2} \lambda_4 (H_1^\dagger H_2 H_1^\dagger H_2 + H_2^\dagger H_1 H_2^\dagger H_1) + \frac{1}{2} \lambda_5 (H_1^\dagger H_2 + H_2^\dagger H_1) H_1^\dagger H_1 \right. \\ \left. + \frac{1}{2} \lambda_6 (H_1^\dagger H_2 + H_2^\dagger H_1) H_2^\dagger H_2 \right\} + \mathcal{O}\left(\frac{|H|^6}{\Lambda^2}\right)$$

9 real constants (in fact 7 independent)

$$\Delta_{jk} \sim \lambda_A \sim N_c$$

Chiral expansion in $1/\Lambda$
in hadron phase of QCD

$$\Lambda \simeq 4\pi F_\pi \sim 4M_{dyn}$$

Bosonization via quasilocal quark models:
2-quark and 4-quark meson states:

A.Andrianov, V.Andrianov et al,
J.Schechter et al

Chirally symmetric parameterization

$$H_1(x) = \sigma_1(x)U(x) = \sigma_1(x)\xi^2(x); \quad \langle H_1 \rangle = \langle \sigma_1 \rangle > 0$$

$$H_2(x) = \xi(x)(\sigma_2(x) + i\hat{\pi}_2(x))\xi(x) = \sigma_2(x)U(x) + i\xi(x)\hat{\pi}_2(x)\xi(x)$$

Effective potential

$$\begin{aligned} V_{\text{eff}} = & - \sum_{j,k=1}^2 \sigma_j \Delta_{jk} \sigma_k - \Delta_{22} (\pi_2^a)^2 \\ & + \lambda_1 \sigma_1^4 + \lambda_2 \sigma_2^4 + (\lambda_3 + \lambda_4) \sigma_1^2 \sigma_2^2 + \lambda_5 \sigma_1^3 \sigma_2 + \lambda_6 \sigma_1 \sigma_2^3 \\ & + (\pi_2^a)^2 \left((\lambda_3 - \lambda_4) \sigma_1^2 + \lambda_6 \sigma_1 \sigma_2 + 2\lambda_2 \sigma_2^2 \right) + \lambda_2 \left((\pi_2^a)^2 \right)^2 \end{aligned}$$

Vacuum states for symmetric baryon matter

A pseudoscalar condensate breaking P-parity?

$$\pi_2^a = \delta^{a0} \rho$$

No! (Vafa-Witten theorem) $\rho = 0$ in QCD at zero quark density

Eqs. for vacuum states

$$2(\Delta_{11}\sigma_1 + \Delta_{12}\sigma_2) = 4\lambda_1\sigma_1^3 + 3\lambda_5\sigma_1^2\sigma_2 + 2(\lambda_3 + \lambda_4)\sigma_1\sigma_2^2 + \lambda_6\sigma_2^3 \\ + \rho^2(2(\lambda_3 - \lambda_4)\sigma_1 + \lambda_6\sigma_2),$$

$$2(\Delta_{12}\sigma_1 + \Delta_{22}\sigma_2) = \lambda_5\sigma_1^3 + 2(\lambda_3 + \lambda_4)\sigma_1^2\sigma_2 + 3\lambda_6\sigma_1\sigma_2^2 + 4\lambda_2\sigma_2^3 \\ + \rho^2(\lambda_6\sigma_1 + 4\lambda_2\sigma_2),$$

$$0 = 2\pi_2^a \left(-\Delta_{22} + (\lambda_3 - \lambda_4)\sigma_1^2 + \lambda_6\sigma_1\sigma_2 + 2\lambda_2\sigma_2^2 + 2\lambda_2\rho^2 \right)$$

Necessary and sufficient condition to avoid P-parity breaking in normal QCD vacuum ($\mu = 0$)

$$(\lambda_3 - \lambda_4)\sigma_1^2 + \lambda_6\sigma_1\sigma_2 + 2\lambda_2\sigma_2^2 > \Delta_{22} \quad \lambda_2 > 0$$

positive mass of $\pi(1300)$

Search for stable “nuclear matter”

4-parameters of linear transformations

$$\tilde{H}_j = \sum_{k=1,2} L_{jk} H_k.$$

are sufficient to provide

$$\Delta_{jk} = \Delta \delta_{jk} \text{ and } \lambda_5 = 0$$

One of the solution of the simplified equations is $\sigma_2 = 0$ and $\sigma_1^2 = \Delta/2\lambda_1$ provided that $\lambda_3 \pm \lambda_4 > 2\lambda_1 > 0$.

It is a minimum!

If $\sigma_2 \neq 0$, another set of solutions for σ_i given in term of the ratio $x \equiv \sigma_2/\sigma_1$

$$2\lambda_1 - (\lambda_3 + \lambda_4) - \frac{3}{2}\lambda_6 x + (\lambda_3 + \lambda_4 - 2\lambda_2)x^2 + \frac{1}{2}\lambda_6 x^3 = 0.$$

This equation may have one or three real roots.

We need three roots!

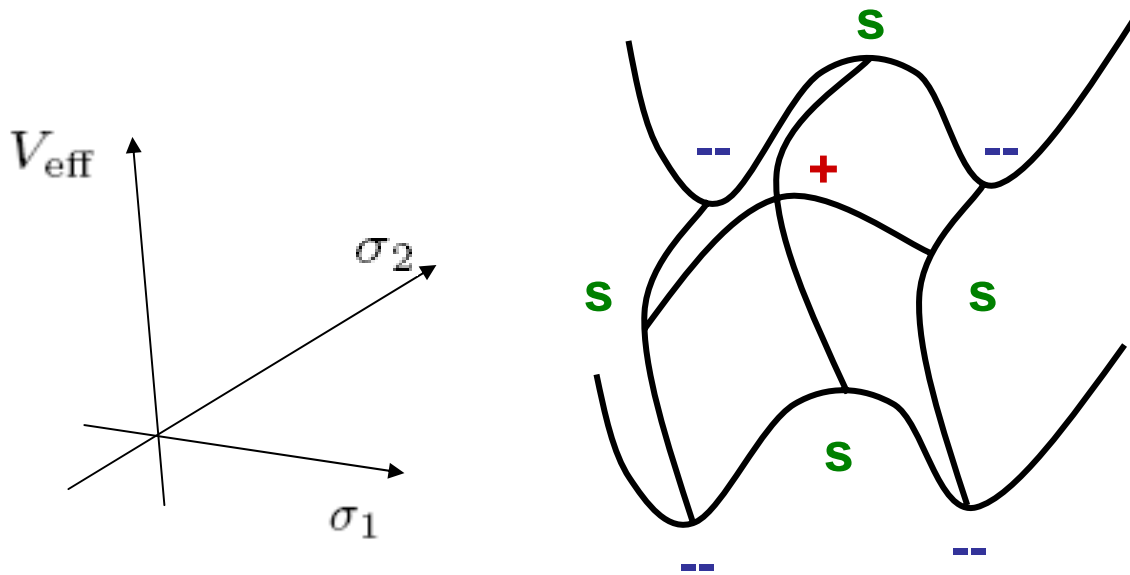
Conditions: $\lambda_6 < 0$, $(\lambda_3 + \lambda_4)\Delta_{22} > 2\lambda_2\Delta_{11}$, $\lambda_3^2 - \lambda_4^2 > 4\lambda_1\lambda_2$.

Landscape of solutions

One negative root – **saddle point**,
two positive roots – **one minimum** and **one saddle point**

effective potential is symmetric against the transformation $\sigma_j \rightarrow -\sigma_j$

→ 9 extremums = 4 **minima** + 4 **saddle points** + 1 **maximum** at the origin



Fix the sign of σ_1 → two competitive minima → phase transition of 1st order

Embedding a chemical potential into “quark matter free energy”

$$\langle N^\dagger N \rangle \iff \int d^3x \mu_B (\bar{N} \gamma_0 N(x) - \rho_B)$$

Local coupling to quarks

$$\mathcal{L}_{int} = -(\bar{q}_R H_1 q_L + \bar{q}_L H_1^\dagger q_R)$$

Superposition of physical meson states

From a quark model

$$\Delta V_{\text{eff}}(\mu) = \frac{\mathcal{N}}{2} \Theta(\mu - |H_1|) \left[\mu |H_1|^2 \sqrt{\mu^2 - |H_1|^2} - \frac{2\mu}{3} (\mu^2 - |H_1|^2)^{3/2} - |H_1|^4 \ln \frac{\mu + \sqrt{\mu^2 - |H_1|^2}}{|H_1|} \right] \left(1 + O\left(\frac{\mu^2}{\Lambda^2}\right) \right)$$

$$\mathcal{N} \equiv \frac{N_c N_f}{4\pi^2}$$

Monotonous function

Only the first Eq. for stationary points is modified

$$2(\Delta_{11}\sigma_1 + \Delta_{12}\sigma_2) = 4\lambda_1\sigma_1^3 + 3\lambda_5\sigma_1^2\sigma_2 + 2(\lambda_3 + \lambda_4)\sigma_1\sigma_2^2 + \lambda_6\sigma_2^3$$

$$+ \rho^2 \left(2(\lambda_3 - \lambda_4)\sigma_1 + \lambda_6\sigma_2 \right) + 2\mathcal{N}\Theta(\mu - \sigma_1) \left[\mu\sigma_1\sqrt{\mu^2 - \sigma_1^2} - \sigma_1^3 \ln \frac{\mu + \sqrt{\mu^2 - \sigma_1^2}}{\sigma_1} \right]$$

$$\equiv \sigma_1 \mathcal{A}(\sigma_1, \mu)$$

Repulsive forces are wanted for stabilization!

Chemical potential triggers condensation of omega mesons

$$\Delta\mathcal{L}_\omega = -\frac{1}{4}\omega_{\mu\nu}\omega^{\mu\nu} + \frac{1}{2}m_\omega^2\omega_\mu\omega^\mu - g_{\omega\bar{q}q}\bar{q}\gamma_\mu\omega^\mu q,$$

Constant v.e.v. $g_{\omega\bar{q}q}\langle\omega_0\rangle \equiv \bar{\omega}$. Shift $\mu \rightarrow \mu + \bar{\omega} \equiv \bar{\mu}$.

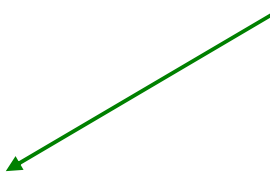
Modification of effective potential

$$\Delta V_\omega = -\frac{1}{2}m_\omega^2\langle\omega_0^2\rangle = -\frac{1}{2}\frac{(\bar{\mu} - \mu)^2}{G_\omega}, \quad G_\omega \equiv \frac{g_{\omega\bar{q}q}^2}{m_\omega^2} \simeq \mathcal{O}\left(\frac{1}{N_c}\right).$$

Stationary solution $\frac{\bar{\mu} - \mu}{G_\omega} = -N_c\rho_B(\mu) = -\frac{N_c N_f}{3\pi^2}(\bar{\mu}^2 - \sigma_1(\bar{\mu})^2)^{3/2}.$

Extension to Hot and Dense matter:

replace

$$\mathcal{A}(\sigma_1, \mu)$$

$$\mathcal{A}(\sigma_1, \mu, \beta) = \int_{\sigma_1}^{\infty} dE \sqrt{E^2 - \sigma_1^2} \frac{\cosh(\beta\mu) + \exp(-\beta E)}{\cosh(\beta\mu) + \cosh(\beta E)} + \mathcal{O}(\mu^2/\Lambda^2, \sigma_1^2/\Lambda^2).$$

after summing up Matsubara frequencies in **one quark loop**

On classical solutions

$$V_{\text{eff}}(\mu) = -\frac{1}{2} \sum_{j,k=1}^2 \sigma_j(\mu) \Delta_{jk} \sigma_k(\mu) - \frac{1}{2} \Delta_{22} \rho^2(\mu) - \frac{\mathcal{N}}{3} \mu \left(\mu^2 - \sigma_1(\mu)^2 \right)^{3/2} \theta(\mu - \sigma_1(\mu))$$
$$+ \Delta V_{\omega}(\bar{\mu}, \mu)$$

Thermodynamic properties at zero temperature

Pressure

$$p(\sigma_j(\mu), \mu) \equiv V_{\text{eff}}(\sigma_j^0) - V_{\text{eff}}(\sigma_j(\mu), \rho(\mu), \mu),$$

$$\partial_\mu p = N_c \varrho_B.$$

Energy density

$$\varepsilon = -p + N_c \mu \varrho_B.$$

relation between baryon density, Fermi momenta and the chemical potential is for quark matter

$$\varrho_B = -\frac{1}{N_c} \partial_\mu V_{\text{eff}} = \frac{N_f}{3\pi^2} p_F^3 = \frac{N_f}{3\pi^2} (\mu^2 - \sigma_1(\mu)^2)^{3/2}.$$

Pressure vanishes in vacuum and at a minimum of energy per baryon

$$p = \varrho_B^2 \partial_{\varrho_B} \left(\frac{\varepsilon}{\varrho_B} \right),$$

This minimum realizes the **stable baryon matter**. Since pressure is increasing with density the phase diagram in the p, ϱ_B plane must necessarily exhibit discontinuity – **1st order phase transition “vapor-liquid”**.

It occurs at $\bar{\mu}^* < \sigma_1^0, \sigma_j^* \equiv \sigma_j(\bar{\mu}^*)$

To realize it one needs **two competitive minima** in the effective potential in order to interchange them at a phase transition point.

Saturation point (phase transition at $p = 0$)

$$\sum_{j,k=1}^2 \left(\sigma_j^0 \Delta_{jk} \sigma_k^0 - \sigma_j^* \Delta_{jk} \sigma_k^* \right) = \frac{N_c N_f}{6\pi^2} \bar{\mu}^* p_F^3(\bar{\mu}^*) + G_\omega \frac{N_c^2 N_f^2}{9\pi^4} p_F^6(\bar{\mu}^*)$$

$$= \frac{N_c}{2} \bar{\mu}^* \varrho_B(\mu^*) + G_\omega N_c^2 \varrho_B^2(\mu^*),$$

$$\mu_* \simeq 303 \text{ MeV}$$

$$G_\omega \sim (10 \div 15) \text{ GeV}^{-2}$$

In hot medium



$$\sum_{j,k=1}^2 \left(\sigma_j^0(\mu^*, T) \Delta_{jk} \sigma_k^0(\mu^*, T) - \sigma_j^*(\mu^*, T) \Delta_{jk} \sigma_k^*(\mu^*, T) \right) = \frac{N_c}{2} \bar{\mu}^* \left(\varrho_B(\beta, \mu^*, \sigma_1^*) - \varrho_B(\beta, \mu^*, \sigma_1^0) \right)$$

$$+ \frac{1}{2} T \left(S(\beta, \mu^*, \sigma_1^*) - S(\beta, \mu^*, \sigma_1^0) \right) + G_\omega N_c^2 \left(\varrho_B^2(\beta, \mu^*, \sigma_1^*) - \varrho_B^2(\beta, \mu^*, \sigma_1^0) \right),$$

Gas-vapor tricritical point for nuclear matter arises
when two minima give the same baryon density
! Two constraints on coupling constants!

Necessary conditions to approach to P-violation phase

$$\partial_\mu \left[(\lambda_3 - \lambda_4) \sigma_1^2 + \lambda_6 \sigma_1 \sigma_2 + 2\lambda_2 \sigma_2^2 \right] < 0$$

or

$$\left(\lambda_6 \sigma_1 + 4\lambda_2 \sigma_2 \right) V_{\sigma_1 \sigma_2}^{(2)} < \left(2(\lambda_3 - \lambda_4) \sigma_1 + \lambda_6 \sigma_2 \right) V_{\sigma_2 \sigma_2}^{(2)}$$

One condition for 7 parameters:

P-violation is not exceptional but rather typical!

The type of phase transition: **it is of a second order**

$$\partial_\mu \sigma_1 \Big|_{\mu_{crit} + i0} - \partial_\mu \sigma_1 \Big|_{\mu_{crit} - i0} = -4\mathcal{N} \sigma_1 \sqrt{\mu^2 - \sigma_1^2} \frac{(\mathcal{V}_{10} \mathcal{V}_{22} - \mathcal{V}_{20} \mathcal{V}_{12})^2}{\text{Det} \mathcal{V} \text{Det} V_\sigma^{(2)}} \Big|_{\rho \rightarrow 0} < 0,$$

Second variation matrices for effective potential **before** and **after** phase transition

P-parity violation phase

Critical points μ_c when $\rho(\mu_c) = 0$

$$(4\lambda_2\Delta_{12} - \lambda_6\Delta_{22})x^2 + (2\lambda_6\Delta_{12} - 4\lambda_4\Delta_{22})x + 2(\lambda_3 - \lambda_4)\Delta_{12} - \lambda_5\Delta_{22} = 0,$$

For $x = \frac{\sigma_2}{\sigma_1}.$

There are in general two solutions for two $\mu_c^- < \mu_c^+$

solution for $\mu > \mu_{crit}$

$$\sigma_2 = A\sigma_1 + \frac{B}{\sigma_1}, \quad A \equiv \frac{2\lambda_5\lambda_2 + \lambda_6(\lambda_4 - \lambda_3)}{\lambda_6^2 - 8\lambda_2\lambda_4}, \quad B \equiv \frac{\lambda_6\Delta_{22} - 4\lambda_2\Delta_{12}}{\lambda_6^2 - 8\lambda_2\lambda_4}.$$

P-parity violation strip

Boundary of the P-breaking phase,

$$\mathcal{N}\mathcal{A}(\sigma_1^\pm, \mu_c^\pm, \beta) = \Delta_{11} - 2\lambda_1(\sigma_1^\pm)^2 - \lambda_5\sigma_1^\pm\sigma_2^\pm - (\lambda_3 - \lambda_4)(\sigma_2^\pm)^2$$

It defines the P-breaking strip in the $T - \mu$ plane.

$\mathcal{A} > 0$ and $\mathcal{A} \rightarrow \infty$ when $T, \mu \rightarrow \infty$.

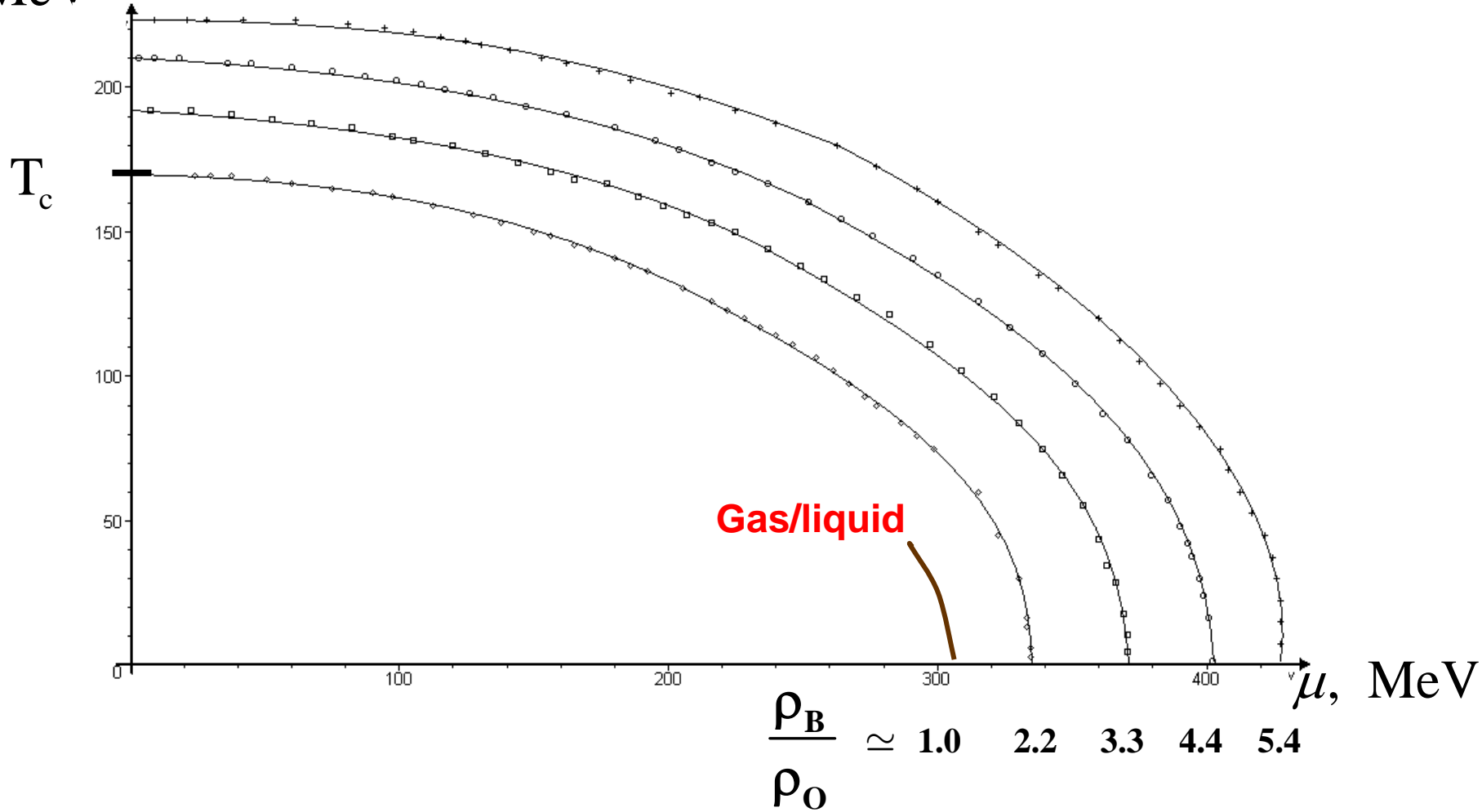
It means that for *any* nontrivial solution $r_\pm, \sigma_1^\pm, \sigma_2^\pm$ with $\mathcal{C}^\pm(\Delta_{jk}, \lambda_j) > 0$ the P-breaking phase boundary exists.

Thus if the phenomenon of P-breaking is realized for zero temperature it will take place in a strip including lower chemical potentials but higher temperatures.

**However within the validity of chiral expansion
the temperature cannot be too high!?**

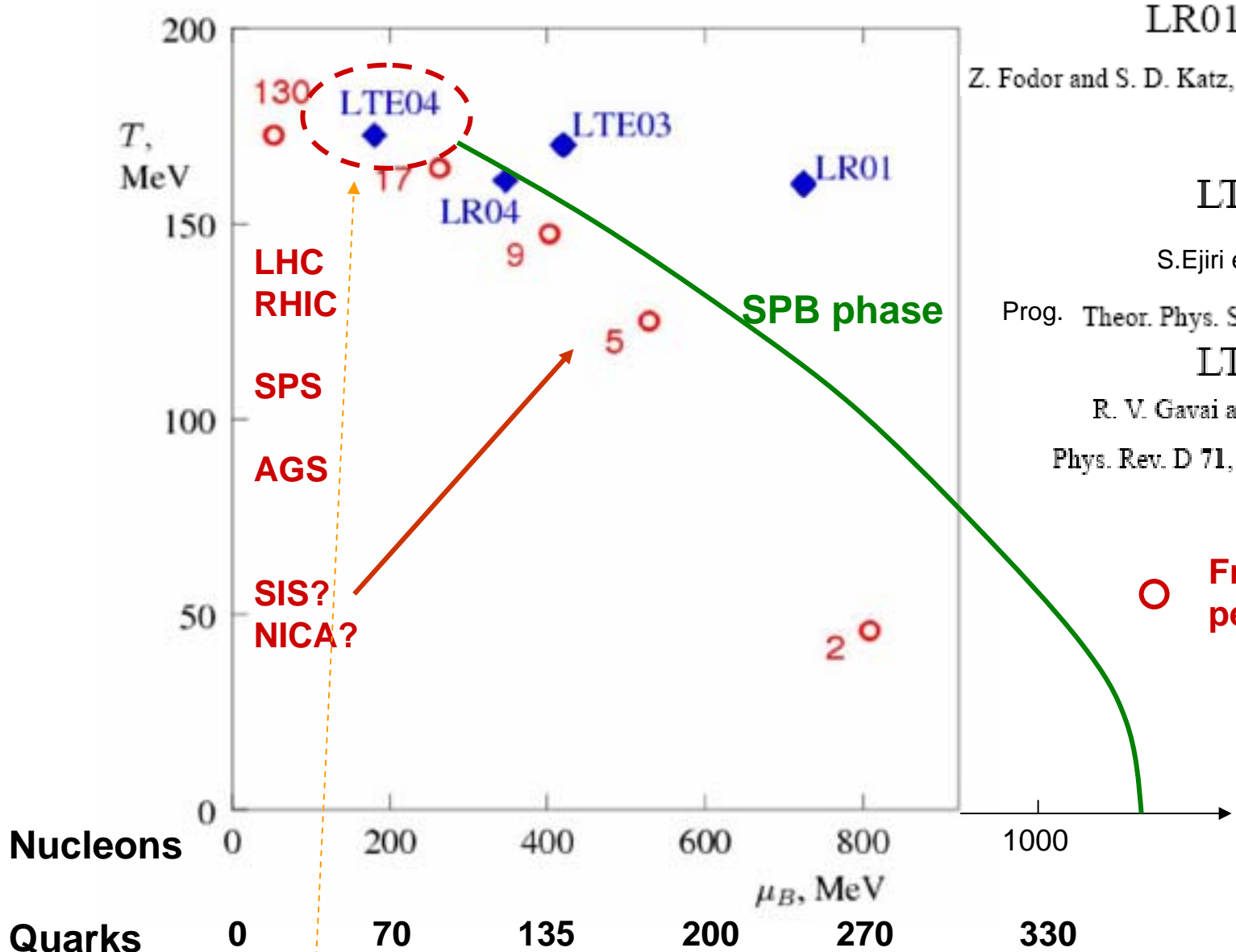
Parity breaking phase divide line

T, MeV



QCD tricritical point

Lattice estimations



LR01, LR04
Z. Fodor and S. D. Katz, JHEP 0203 (2002) 014
JHEP 0404, 050 (2004)

LTE03

S.Ejiri et al.

Prog. Theor. Phys. Suppl. 153, 118 (2004)

LTE04

R. V. Gavai and S. Gupta,

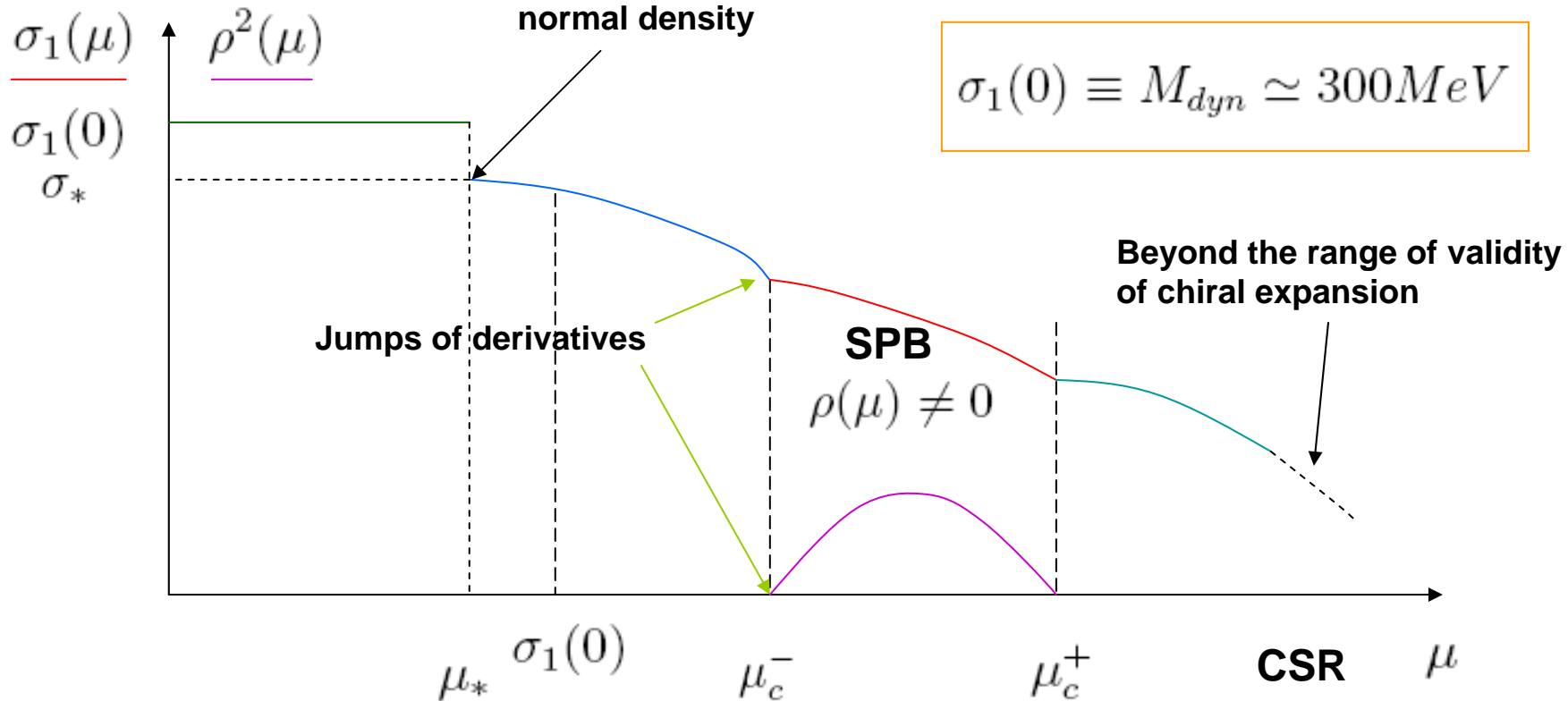
Phys. Rev. D 71, 114014 (2005)

○ Freezout energy per baryon

!! $\mu_B^{\text{cep}} \sim 150 - 180$ MeV and $T_{\text{cep}} \sim 165 - 170$ MeV

R.A.Lacey et al 0708.3512, elliptic flow v2

I^d order phase transition to saturation point (normal nuclear density) and spontaneous P-parity breaking (II^d order phase transition)



With increasing μ one enters SPB phase and leaves it before (?) encountering any new phase (CSR, CFL ...)

P-breaking phase

Partially diagonalized kinetic term

$$\begin{aligned}
 \mathcal{L}_{kin}^{(2)} = & \partial_\mu \tilde{\pi}^\pm \partial^\mu \tilde{\pi}^\mp + (A_{22} - \zeta^2) \partial_\mu \Pi^\pm \partial^\mu \Pi^\mp + \frac{1}{2} \left(1 + \frac{A_{22} \rho^2}{F_0^2} \right) \partial_\mu \tilde{\pi}^0 \partial^\mu \tilde{\pi}^0 \\
 & + \frac{1}{2} \left(A_{22} - \frac{F_0^2}{F_0^2 + A_{22} \rho^2} \zeta^2 \right) \partial_\mu \Pi^0 \partial^\mu \Pi^0 + \frac{1}{2} \sum_{j,k=1}^2 \frac{A_{jk} F_0^2 + \rho^2 \det A \delta_{1j} \delta_{1k}}{F_0^2 + A_{22} \rho^2} \partial_\mu \Sigma_j \partial^\mu \Sigma_k \\
 & - \frac{F_0 \rho}{F_0^2 + A_{22} \rho^2} \zeta \partial_\mu \Pi^0 \sum_{j=1}^2 A_{j2} \partial^\mu \Sigma_j
 \end{aligned}$$

Isospin breaking $SU_V(2) \rightarrow U(1)$

Meson spectrum in SPB phase

Neutral pi-prime condensate breaks vector SU(2) to U(1)
and **two charged pi-prime mesons become massless**

$$\frac{1}{2}V_{11}^{(2)\sigma} = 4\lambda_1\sigma_1^2 + 2\lambda_5\sigma_1\sigma_2 + 2\lambda_4\sigma_2^2 - 2\mathcal{N}\sigma_1^2 \ln \frac{\mu + \sqrt{\mu^2 - \sigma_1^2}}{\sigma_1}$$

$$V_{12}^{(2)\sigma} = 2\lambda_5\sigma_1^2 + 4\lambda_3\sigma_1\sigma_2 + 2\lambda_6\sigma_2^2$$

$$\frac{1}{2}V_{22}^{(2)\sigma} = 2\lambda_4\sigma_1^2 + 2\lambda_6\sigma_1\sigma_2 + 4\lambda_2\sigma_2^2$$

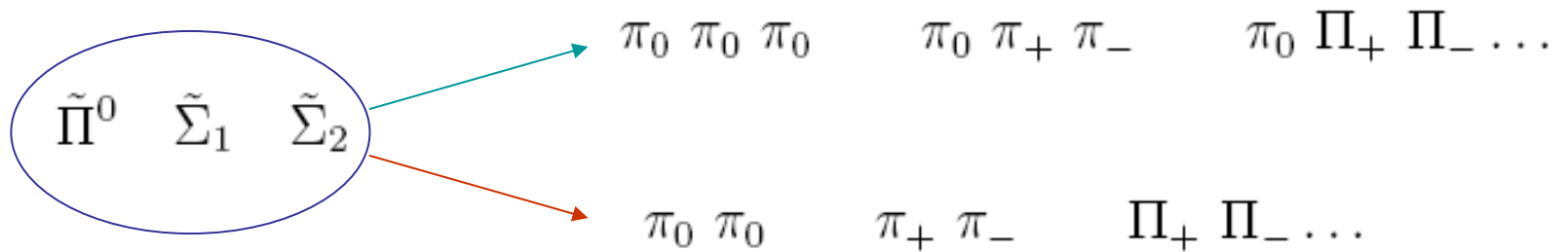
$$\left. \begin{aligned} V_{10}^{(2)\sigma\pi} &= \left(4(\lambda_3 - \lambda_4)\sigma_1 + 2\lambda_6\sigma_2\right)\rho \\ V_{20}^{(2)\sigma\pi} &= \left(2\lambda_6\sigma_1 + 8\lambda_2\sigma_2\right)\rho \end{aligned} \right\} \text{Mixture of massive scalar and neutral pseudoscalar states}$$

$$\frac{1}{2}V_{00}^{(2)\pi} = 4\lambda_2\rho^2 \quad \boxed{\frac{1}{2}V_{\pm\mp}^{(2)\pi} = 0}$$

Mass matrix diagonalization $\Pi^0 \quad \Sigma_1 \quad \Sigma_2 \implies \tilde{\Pi}^0 \quad \tilde{\Sigma}_1 \quad \tilde{\Sigma}_2$

mixes neutral pseudoscalar and scalar states

Therefore genuine mass states don't possess a definite parity in decays

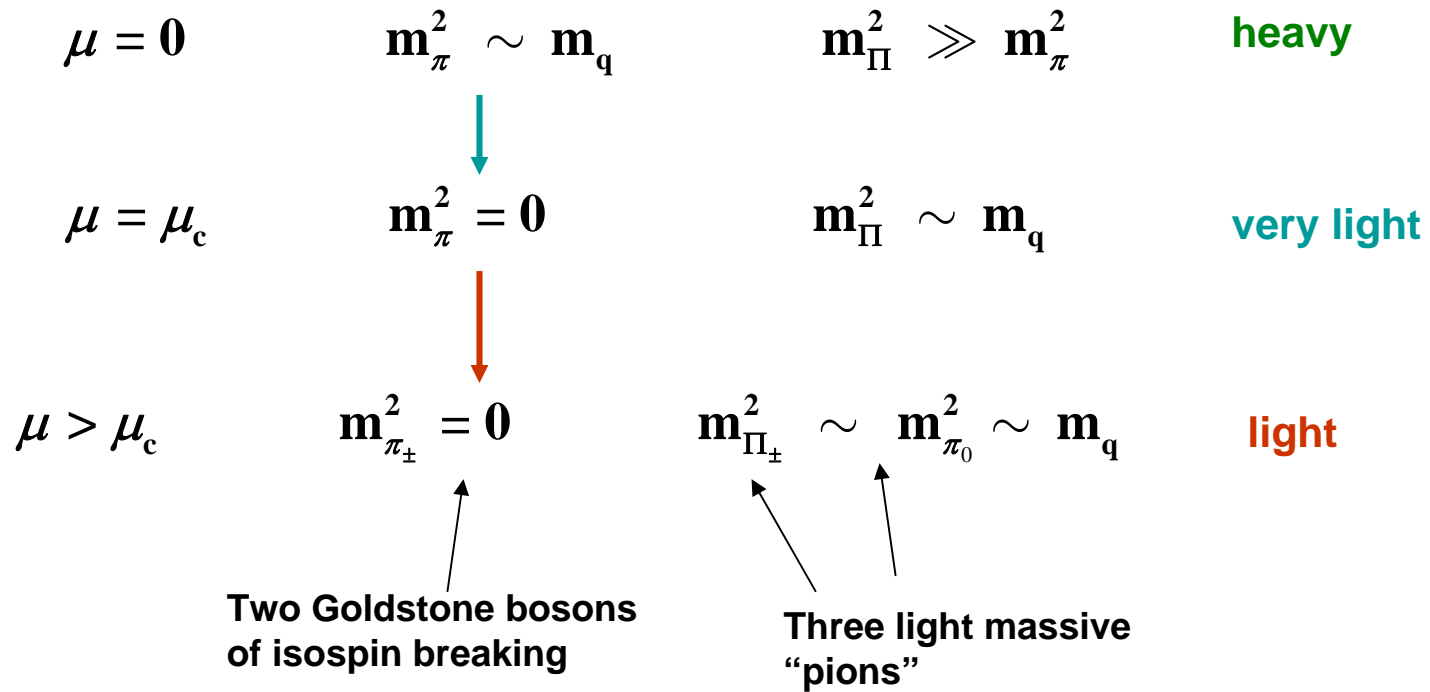


Beyond the chiral limit: $m_q \neq 0$

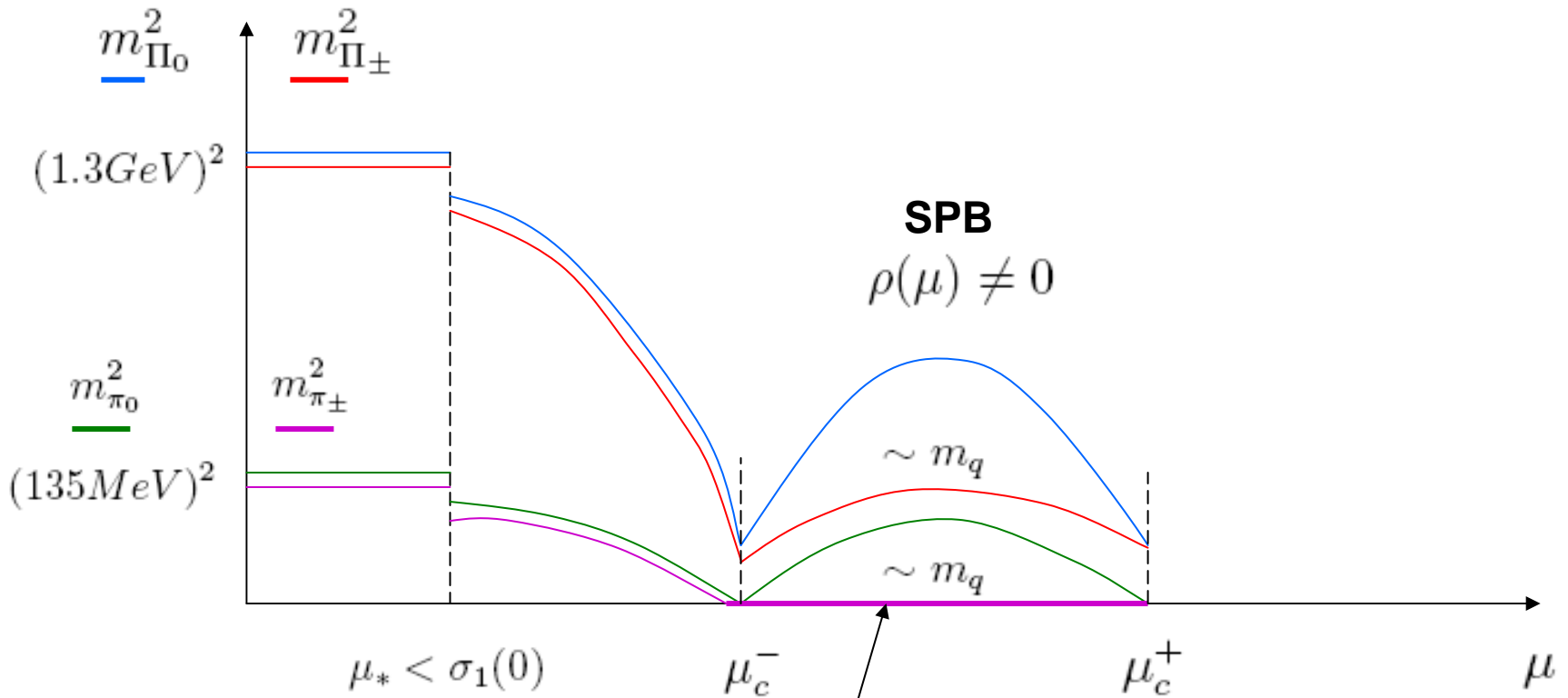
Two new lowest-dimensional operators

$$\frac{1}{2}m_q d_1 \text{tr}(H_1 + H_1^\dagger) \qquad \frac{1}{2}m_q d_2 \text{tr}(H_2 + H_2^\dagger)$$

The spectrum in dense matter



Mass spectrum of “pseudoscalar” states (massive quarks)



In P-breaking phase there are 2 massless pseudoscalar mesons

$\tilde{\pi}_{\pm}$

Where to see and how to check SPV ?

- a) Approaching to SPV phase is indicated by a rapid decrease in heavy resonance masses . Below phase transition point one finds an abnormally ***light and long-living pseudoscalar in-medium resonances!***
- b) At the very point of the P-breaking phase transition one has three massless (very light) pion-like state.
- c) After phase transition two massless (very light) charged pseudoscalars remain as Goldstone bosons enhancing charged pion production .

Hunting for new light pseudoscalars in medium!

- d) F_{Π} and extended PCAC: it is modified for massless charged pions giving an enhancement of electroweak decays of heavy pions.
 - e) Additional isospin breaking: $f_{\pi_0} \neq f_{\pi_{\pm}}$
-

Perspectives

One can search for enhancement of long-range correlations in the pseudoscalar channel in lattice simulations? $T \neq 0$; $\text{Im } \mu \neq 0$

Program for GSI SIS 300 ? For NICA, Dubna ?

Back side slides

Converter of collider energies per NN into phase diagram

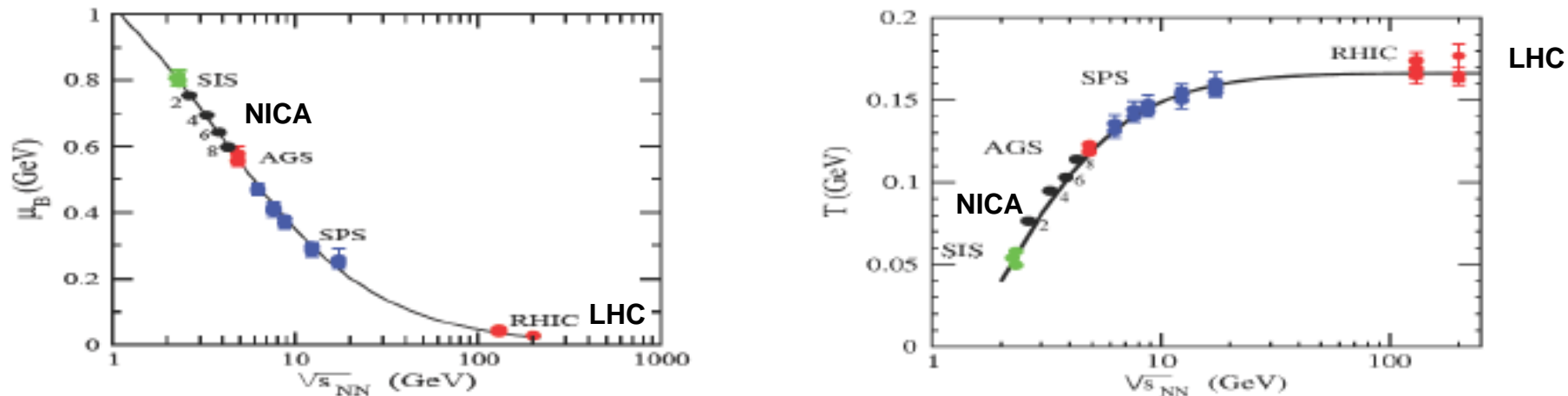


FIG. 1: (Color online) $\sqrt{s_{NN}}$ dependence of μ_B (top panel) and T obtained from chemical fits [20] to particle yield ratios obtained at different accelerator facilities as indicated. The solid lines are fits to these data.

NICA, Dubna, 2014?

Estimations of coupling constants in Quasilocal Quark Model

$$\mathcal{L}_{\text{QQM}} = \bar{q}(i\not{\partial})q + \sum_{k,l=1}^2 a_{kl} [\bar{q}f_k(s)q\bar{q}f_l(s)q - \bar{q}f_k(s)\tau^a\gamma_5q\bar{q}f_l(s)\tau^a\gamma_5q]. \quad (3)$$

Here a_{kl} represents a symmetric matrix of real coupling constants and $f_k(s)$, $s \equiv -\partial^2/\Lambda^2$ are the polynomial form factors specifying the quasilocal (in momentum space) interaction. The form factors are orthogonal on the unit interval and the results of calculations do not depend on a concrete choice of form factors in the large-log approximation. A convenient choice is $f_1(s) = 2 - 3s$, $f_2(s) = -\sqrt{3}s$. The values of couplings λ_i in Eq. (2) are then fixed for $i = 2, \dots, 6$: $\lambda_2 = \frac{9N_c}{32\pi^2}$, $\lambda_3 = \frac{3N_c}{8\pi^2}$, $\lambda_4 = \frac{3N_c}{16\pi^2}$, $\lambda_5 = -\frac{5\sqrt{3}N_c}{8\pi^2}$, $\lambda_6 = \frac{\sqrt{3}N_c}{8\pi^2}$.

λ_1 is rather arbitrary

P-parity violation is possible!

A bit of history: pion condensation in symmetric nuclear matter $\rho_p = \rho_n$

A. Migdal, 1971

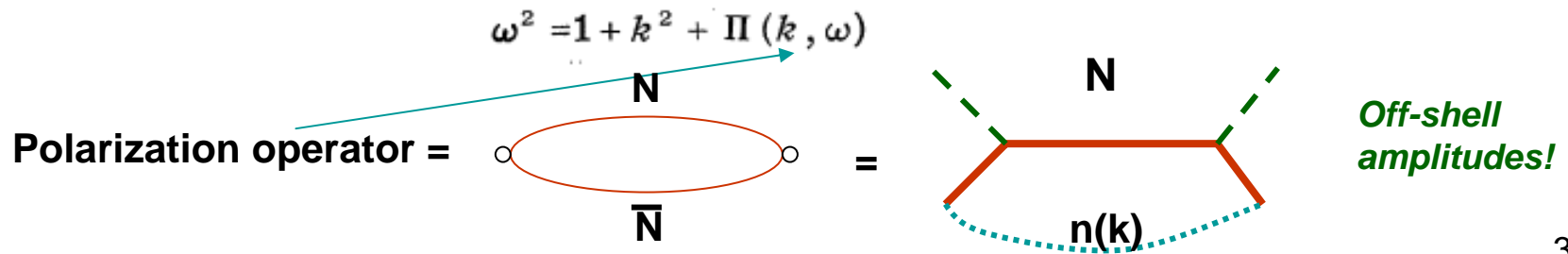
$$\omega^2 = 1 + k^2 - 4\pi n F(k) \quad \leftarrow \quad \hbar = c = m_\pi = 1$$

where n is the nucleon density and $F(k)$ is the forward pion-nucleon scattering amplitude *which* for both π^+ and π^- mesons, has the sign corresponding to attraction ($F > 0$), and therefore at sufficient density the frequency can vanish, meaning instability of the pion field. However, $F(k)$ is small at small k and instability sets in at $k = k_0$, which corresponds to the minimal value of $k^2 - 4\pi n F(k)$. The instability condition is $\omega^2 = 0$ or

$$1 + k_0^2 = 4\pi n F(k_0)$$

In this approach a pion condensate is spatially inhomogeneous!

A more exact calculation includes the particle-hole excitations of the nuclear medium



Polarization operator in details

$$\Pi^{(1)\pi^-}(\omega, k) = -2 \int \frac{d^3p}{(2\pi)^3} [D_{\pi^-n}(\omega, k)n_n(p) + D_{\pi^-p}(\omega, k)n_p(p)],$$

where D_{π^-n} and D_{π^-p} are the spin-averaged forward scattering amplitudes, $n_n(p)$ and $n_p(p)$ are the occupation functions of the neutrons and the protons respectively,

$$\Pi^{(1)\pi^-}(\omega, k; \rho) = \Pi_N^{(1)\pi^-} + \Pi_\Delta^{(1)\pi^-} + \Pi_D^{(1)\pi^-} + \Pi_\sigma^{(1)\pi^-}$$

Off-shell amplitudes from an effective lagrangian

where the subscripts N , Δ , D and σ refer to contributions from nucleon exchange, delta exchange, direct pion–nucleon scattering and the pion–nucleon σ term,

Most pessimistic!

T Shamsunnahar et al.

J. Phys. G: Nucl. Part. Phys. **17** (1991) 887

No pion condensate ?

